Math 1071

Name: _

Section: $_$

Fraction Arithmetic

See Appendix A2 for more rules and tricks. Let $b, e \neq 0$ in the following.

| $\frac{a}{b} + \frac{c}{b} = \frac{a+c}{b}$ | $\frac{a}{b} - \frac{c}{b} = \frac{a-c}{b}$ |
|---|---|
| $\frac{a}{b} \cdot \frac{c}{e} = \frac{a \cdot c}{b \cdot e}$ | $\frac{1}{\frac{a}{b}} = \frac{b}{a}$ |
| $rac{a}{b} = rac{a \cdot e}{b \cdot e}$ | $rac{a \cdot c}{b} \; = \; a \cdot rac{c}{b}$ |

Exponential Arithmetic

See Appendix A1 for more rules and tricks. Let a, b > 0 in the following.

$$a^{r+s} = a^{r} \cdot a^{s}$$

$$(a^{r})^{s} = a^{r \cdot s}$$

$$(a \cdot b)^{r} = a^{r} \cdot b^{r}$$

$$a^{s} = \frac{1}{a^{s}}$$

$$a^{s} = \frac{1}{a^{-s}}$$

$$\sqrt[r]{a \cdot b} = \sqrt[r]{a} \cdot \sqrt[r]{b}$$

$$\sqrt[r]{a} = a^{1/r}$$

Fractions which do NOT simplify easily

Doesn't simplify at all: $\frac{3}{x+1}$

Must find a common denomiator before you can combine terms: $\frac{x+1}{x-1} + \frac{1}{x}$

Exponents and Products that do NOT simplify easily

Doesn't simplify at all:

$$\sqrt{x+1} = (x+1)^{1/2}$$

You must FOIL to simplify:

$$(x+1)^2 = (x+1)(x+1) = x^2 + 2x + 1$$

You must rewrite, FOIL, and distribute twice to simplify:

$$(x+1)^3 = (x+1)(x^2+2x+1) = (x+1) \cdot x^2 + (x+1) \cdot 2x + (x+1) \cdot 1$$

